

5-4

Point-Slope Form



Vocabulary

Review

1. Circle the equation that has a *y*-intercept of 3.

$y = 3x + 4$

$y = 4x - 3$

$y = 5x + 3$

$y = -3x + 2$

2. Circle the equation that is in *slope-intercept* form.

$2x - y = 10$

$x + 3y + 11 = 0$

$y - 4 = \frac{2}{3}(x + 7)$

$y = 2x + 6$

3. Circle the statement that is true about the *y*-intercept of any graph.

occurs where $y = 0$
on the graph

occurs where $x = 0$
on the graph

occurs where graph
touches the x -axis

Vocabulary Builder

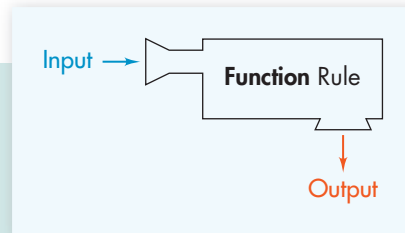
function (noun) FUNGK shun

Related Words: input, output, function rule

Definition: A **function** is a relationship that assigns exactly one output value to each input value.

Main Idea: A **function** is used to describe how one value depends on another.

Example: The function machine above shows that the **function** assigns an **output** to every **input** according to a specified rule.



Use Your Vocabulary

Complete each sentence with the appropriate word from the list.

price

sun

time

4. The length of a shadow is a *function* of the angle of the ? .

5. The amount of water that has leaked from a leaky faucet is a *function* of ? .

6. The amount of sales tax you pay is a *function* of the item's ? .

Key Concept Point-Slope Form of a Linear Equation

The **point-slope form** of an equation of a nonvertical line with slope m and through point (x_1, y_1) is $y - y_1 = m(x - x_1)$.

7. In the above, what does (x_1, y_1) represent?

8. What does m represent?



Problem 1 Writing an Equation in Point-Slope Form

Got It? A line passes through $(8, -4)$ and has slope $\frac{2}{3}$. What is an equation in point-slope form of the line?

9. Use the point-slope form of an equation. For a line that passes through $(8, -4)$ and has slope $\frac{2}{3}$, circle x_1 and underline y_1 .

| | | | |
|----|---------------------------------|---|----|
| -4 | <u>$\frac{2}{3}$</u> | 8 | 12 |
|----|---------------------------------|---|----|

10. Now substitute into point-slope form.

$$y - y_1 = m \cdot (x - x_1)$$

↓ ↓ ↓
 $y - \square = \square \cdot (x - \square)$

11. An equation of the line is .



Problem 2 Graphing Using Point-Slope Form

Got It? What is the graph of the equation $y + 7 = -\frac{4}{5}(x - 4)$?

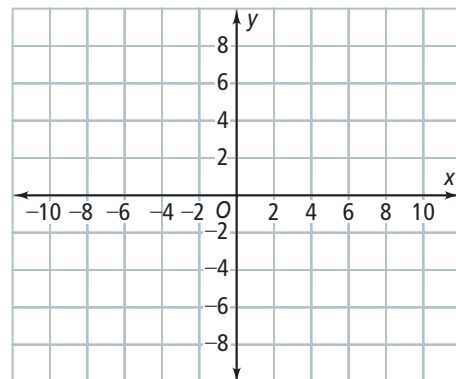
12. Circle the ordered pair of a point on the graph of $y + 7 = -\frac{4}{5}(x - 4)$.

| | | | |
|--------|--------|----------|---------|
| (7, 4) | (4, 7) | (-4, -7) | (4, -7) |
|--------|--------|----------|---------|

13. Circle the correct description of the slope.

| | | |
|--------------------------------|----------------------------------|---------------------------------|
| Go up 4 units and left 5 units | Go down 4 units and left 5 units | Go up 4 units and right 5 units |
|--------------------------------|----------------------------------|---------------------------------|

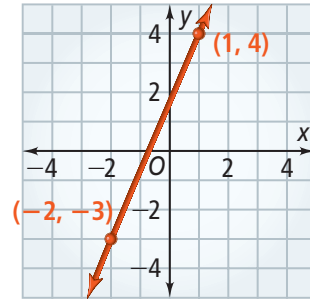
14. Use your answers to Exercises 12 and 13 to graph the line.





Problem 3 Using Two Points to Write an Equation

Got It? Use the point $(-2, -3)$ to write an equation of the line shown.



15. Follow the steps to write the equation of the line shown.

1

Find the slope of the line. Use two points and the

slope formula, $m = \frac{y_2 - y_1}{x_2 - x_1}$.



2

Use the slope and the point $(-2, -3)$ to write an equation of the line in point-slope form.

$$y - y_1 = m(x - x_1)$$

$y - \square = \square \cdot (x - \square)$

An equation of the line is .



Problem 4 Using a Table to Write an Equation

Got It? The table shows the number of gallons of water y in a tank after x hours. The relationship is linear. What is an equation in point-slope form that models the data? What does the slope represent?

Volume of Water in Tank

| Time, x (h) | Water, y (gal) |
|---------------|------------------|
| 2 | 3320 |
| 3 | 4570 |
| 5 | 7070 |
| 8 | 10,820 |

16. Complete the reasoning model below.

| Think | Write |
|--|--|
| I can use any two points from the table to find the slope. | $m = \frac{4570 - \square}{3 - \square} = \frac{\square}{\square}$ |
| Then I can substitute one point and the slope into the point-slope equation. | $y - y_1 = m \cdot (x - x_1)$ $y - \square = \square \cdot (x - \square)$ |
| Finally, I can tell what the slope represents. | The slope represents a rate of <u>?</u> . |

Got It? Reasoning Write the equation from Exercise 16 in slope-intercept form. What does the y -intercept represent?

17. Write the equation in point-slope form from Exercise 16. Use it to write the equation in slope-intercept form.

18. What does the y -intercept in your answer to Exercise 17 represent?



Lesson Check • Do you UNDERSTAND?

Reasoning Can any equation in point-slope form also be written in slope-intercept form? Give an example to explain.

19. Use point-slope form, $y - y_1 = m(x - x_1)$, and any point and slope to write an equation in point-slope form.

20. Now write your equation in slope-intercept form.

21. Can any equation in point-slope form also be written in slope-intercept form?

Yes / No



Math Success

Check off the vocabulary words that you understand.

point-slope form

equation

graph

Rate how well you can *write equations in point-slope form*.

