

5-4 Reteaching

Point-Slope Form

The **point-slope form** of a nonvertical linear equation is $y - y_1 = m(x - x_1)$. In this equation, m is the slope and (x_1, y_1) is a point on the graph of the equation.

Problem

A line passes through $(5, -2)$ and has a slope -3 . What is an equation for this line in point-slope form?

$$y - y_1 = m(x - x_1)$$

$$y - (-2) = -3(x - 5)$$

$$y + 2 = -3(x - 5)$$

Use point-slope form.

Substitute $(5, -2)$ for (x_1, y_1) and -3 for m .

Simplify.

Problem

A line passes through $(1, 4)$ and $(2, 9)$. What is an equation for this line in point-slope form? What is an equation for this line in slope-intercept form? First use the two given points to find the slope.

$$m = \frac{9 - 4}{2 - 1} = \frac{5}{1} = 5$$

Use the slope and one point to write an equation in point-slope form.

$$y - y_1 = m(x - x_1)$$

$$y - 4 = 5(x - 1)$$

$$y - 4 = 5x - 5$$

$$y = 5x - 1$$

Use point-slope form

Substitute $(1, 4)$ for (x_1, y_1) and 5 for m .

Distributive Property

Add 4 to each side.

An equation in point-slope form is $y - 4 = 5(x - 1)$. An equation in slope-intercept form is $y = 5x - 1$.

Exercises

Write an equation for the line through the given point and with the given slope m .

1. $(-1, 3); m = -\frac{1}{4}$

2. $(7, -5); m = 4$

3. $(-2, -5); m = \frac{2}{3}$

Write an equation in point-slope form of the line through the given points. Then write the equation in slope-intercept form.

4. $(1, 4)$ and $(2, 7)$

5. $(2, 0)$ and $(3, -2)$

6. $(4, -5)$ and $(-2, -2)$

5-4 Reteaching (continued)

Point-Slope Form

You can use the point-slope form of an equation to help graph the equation. The point given by the point-slope form provides a place to start on the graph. Plot a point there. Then use the slope from the point-slope form to locate another point in either direction. Then draw a line through the points you have plotted.

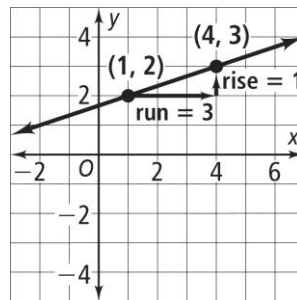
Problem

What is the graph of the equation $y - 2 = \frac{1}{3}(x - 1)$?

The equation is in point-slope form, so the line passes through $(1, 2)$ and has a slope of $\frac{1}{3}$.

Plot the point $(1, 2)$.

Use the slope, $\frac{1}{3}$. From $(1, 2)$, go up 1 unit and then right 3 units. Draw a point.



Draw a line through the two points.

Because $\frac{1}{3} = \frac{-1}{-3}$, you can start at $(1, 2)$ and go down 1 unit and to the left 3 units to locate a third point on the line.

Exercises

Graph each equation.

7. $y - 3 = 2(x + 1)$

8. $y + 2 = \frac{2}{3}(x - 2)$

9. $y - 4 = -\frac{1}{2}(x + 1)$